Core 2: Trapezium Rule

Past Paper Questions 2006 - 2013

Name:

Numerical integration

The trapezium rule: $\int_a^b y \, dx \approx \frac{1}{2} h\{(y_0 + y_n) + 2(y_1 + y_2 + ... + y_{n-1})\}$, where $h = \frac{b-a}{n}$

2 (a) Use the trapezium rule with five ordinates (four strips) to find an approximate value for

$$\int_0^4 \frac{1}{x^2 + 1} \mathrm{d}x$$

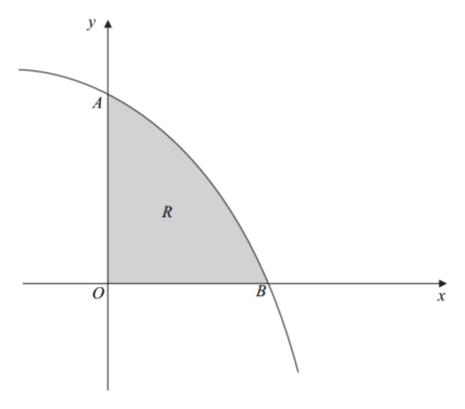
giving your answer to four significant figures.

(4 marks)

(b) State how you could obtain a better approximation to the value of the integral using the trapezium rule. (1 mark)

June 2006

6 The diagram shows a sketch of the curve with equation $y = 27 - 3^x$.



The curve $y = 27 - 3^x$ intersects the y-axis at the point A and the x-axis at the point B.

(a) (i) Find the y-coordinate of point A.

(2 marks)

(ii) Verify that the x-coordinate of point B is 3.

(1 mark)

(b) The region, R, bounded by the curve $y = 27 - 3^x$ and the coordinate axes is shaded. Use the trapezium rule with four ordinates (three strips) to find an approximate value for the area of R. (4 marks)

January 2007

2 Use the trapezium rule with four ordinates (three strips) to find an approximate value for

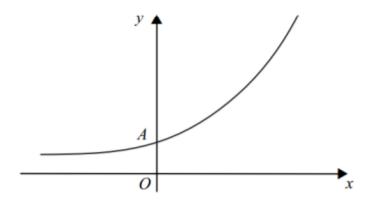
$$\int_0^3 \sqrt{2^x} \, dx$$

giving your answer to three decimal places.

(4 marks)

June 2007

6 The diagram shows a sketch of the curve with equation $y = 3(2^x + 1)$.



The curve $y = 3(2^x + 1)$ intersects the y-axis at the point A.

(a) Find the y-coordinate of the point A.

(2 marks)

(b) Use the trapezium rule with four ordinates (three strips) to find an approximate value for $\int_{0}^{6} 3(2^{x} + 1) dx$. (4 marks)

January 2008

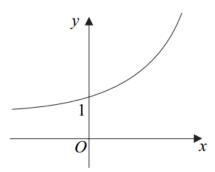
4 Use the trapezium rule with four ordinates (three strips) to find an approximate value for

$$\int_{0}^{3} \sqrt{x^2 + 3} \, dx$$

giving your answer to three decimal places.

(4 marks)

8 The diagram shows a sketch of the curve with equation $y = 6^x$.



- (a) (i) Use the trapezium rule with five ordinates (four strips) to find an approximate value for $\int_0^2 6^x dx$, giving your answer to three significant figures. (4 marks)
 - (ii) Explain, with the aid of a diagram, whether your approximate value will be an overestimate or an underestimate of the true value of $\int_0^2 6^x dx$. (2 marks)

January 2009

2 (a) Use the trapezium rule with four ordinates (three strips) to find an approximate value for

$$\int_{1.5}^{6} x^2 \sqrt{x^2 - 1} \, \mathrm{d}x$$

giving your answer to three significant figures.

(4 marks)

(b) State how you could obtain a better approximation to the value of the integral using the trapezium rule. (1 mark)

June 2009

4 (a) Use the trapezium rule with four ordinates (three strips) to find an approximate value for $\int_0^6 \sqrt{x^3 + 1} \, dx$, giving your answer to four significant figures. (4 marks)

January 2010

- 6 (b) (i) Use the trapezium rule with five ordinates (four strips) to find an approximate value for $\int_0^2 2^x dx$, giving your answer to three significant figures. (4 marks)
 - (ii) State how you could obtain a better approximation to the value of the integral using the trapezium rule. (1 mark)

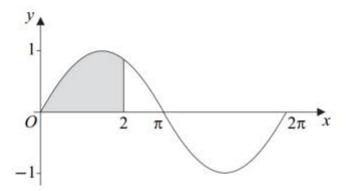
Use the trapezium rule with six ordinates (five strips) to find an approximate value for $\int_0^1 2^{4x} dx$, giving your answer to two decimal places. (4 marks)

January 2011

4 (a) Use the trapezium rule with four ordinates (three strips) to find an approximate value for $\int_0^{1.5} \sqrt{27x^3 + 4} \, dx$, giving your answer to three significant figures. (4 marks)

June 2011

A curve C, defined for $0 \le x \le 2\pi$ by the equation $y = \sin x$, where x is in radians, is sketched below. The region bounded by the curve C, the x-axis from 0 to 2 and the line x = 2 is shaded.



(a) The area of the shaded region is given by $\int_0^2 \sin x \, dx$, where x is in radians.

Use the trapezium rule with five ordinates (four strips) to find an approximate value for the area of the shaded region, giving your answer to three significant figures.

(4 marks)

January 2012

2 (a) Use the trapezium rule with five ordinates (four strips) to find an approximate value for

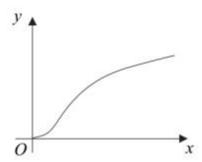
$$\int_0^4 \frac{2^x}{x+1} \, \mathrm{d}x$$

giving your answer to three significant figures.

(4 marks)

(b) State how you could obtain a better approximation to the value of the integral using the trapezium rule. (1 mark)

9 The diagram shows part of a curve whose equation is $y = \log_{10}(x^2 + 1)$.



(a) Use the trapezium rule with five ordinates (four strips) to find an approximate value for

$$\int_0^1 \log_{10}(x^2 + 1) \, \mathrm{d}x$$

giving your answer to three significant figures.

(4 marks

January 2013

2 (a) Use the trapezium rule with five ordinates (four strips) to find an approximate value for

$$\int_{1}^{5} \frac{1}{x^2 + 1} \, \mathrm{d}x$$

giving your answer to three significant figures.

(4 marks)