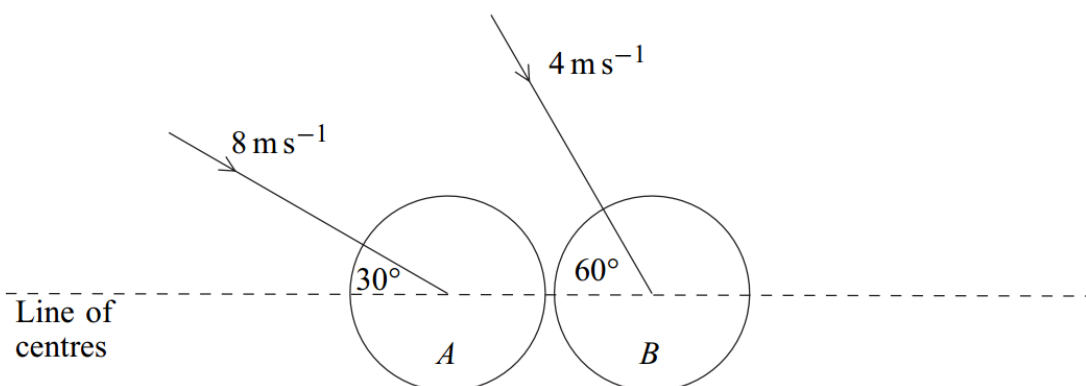

M3: Collisions in 1D

Past Paper Questions
2006 - 2013

Name:

- 6 Two smooth billiard balls A and B , of identical size and equal mass, move towards each other on a horizontal surface and collide. Just before the collision, A has velocity 8 m s^{-1} in a direction inclined at 30° to the line of centres of the balls, and B has velocity 4 m s^{-1} in a direction inclined at 60° to the line of centres, as shown in the diagram.

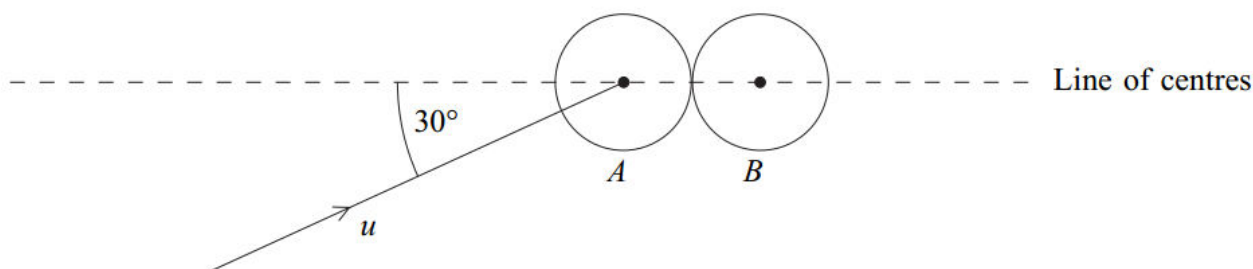


The coefficient of restitution between the balls is $\frac{1}{2}$.

- (a) Find the speed of B immediately after the collision. (9 marks)
- (b) Find the angle between the velocity of B and the line of centres of the balls immediately after the collision. (2 marks)

- 6 A smooth spherical ball, A , is moving with speed u in a straight line on a smooth horizontal table when it hits an identical ball, B , which is at rest on the table.

Just before the collision, the direction of motion of A makes an angle of 30° with the line of the centres of the two balls, as shown in the diagram.



The coefficient of restitution between A and B is e .

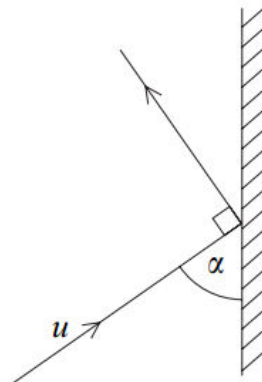
- (a) Given that $\cos 30^\circ = \frac{\sqrt{3}}{2}$, show that the speed of B immediately after the collision is

$$\frac{\sqrt{3}}{4}u(1 + e) \quad (5 \text{ marks})$$

- (b) Find, in terms of u and e , the components of the velocity of A , parallel and perpendicular to the line of centres, immediately after the collision. (3 marks)
- (c) Given that $e = \frac{2}{3}$, find the angle that the velocity of A makes with the line of centres immediately after the collision. Give your answer to the nearest degree. (3 marks)

- 6 A small smooth ball of mass m , moving on a smooth horizontal surface, hits a smooth vertical wall and rebounds. The coefficient of restitution between the wall and the ball is $\frac{3}{4}$.

Immediately before the collision, the ball has velocity u and the angle between the ball's direction of motion and the wall is α . The ball's direction of motion immediately after the collision is at right angles to its direction of motion before the collision, as shown in the diagram.

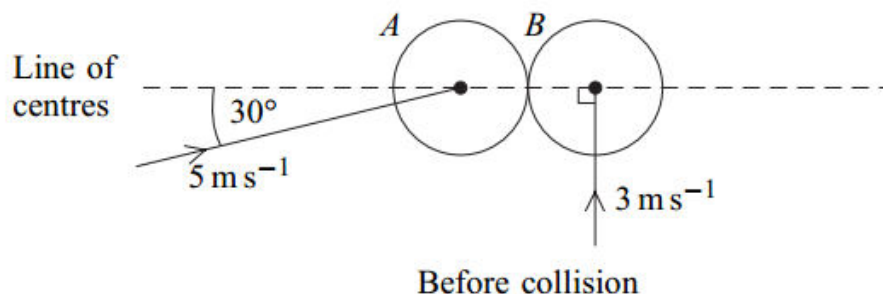


- (a) Show that $\tan \alpha = \frac{2}{\sqrt{3}}$. (5 marks)
- (b) Find, in terms of u , the speed of the ball immediately after the collision. (2 marks)
- (c) The force exerted on the ball by the wall acts for 0.1 seconds.

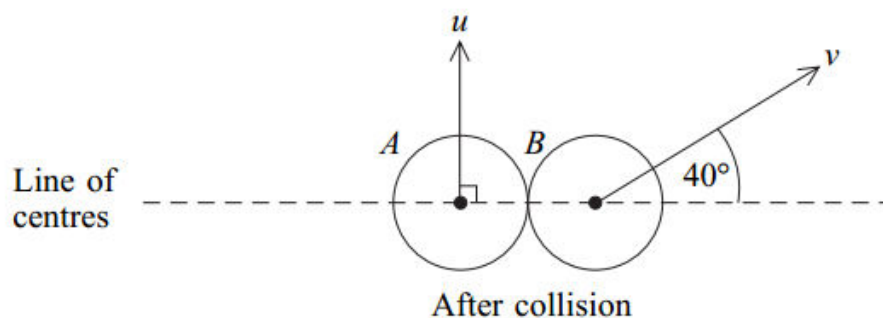
Given that $m = 0.2 \text{ kg}$ and $u = 4 \text{ m s}^{-1}$, find the average force exerted by the wall on the ball. (6 marks)

- 5 Two smooth spheres, A and B , of equal radii and different masses are moving on a smooth horizontal surface when they collide.

Just before the collision, A is moving with speed 5 m s^{-1} at an angle of 30° to the line of centres, and B is moving with speed 3 m s^{-1} perpendicular to the line of centres, as shown in the diagram below.



Immediately after the collision, A and B move with speeds u and v in directions which make angles of 90° and 40° respectively with the line of centres, as shown in the diagram below.



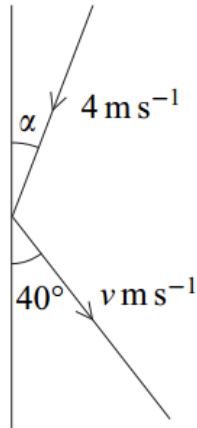
- (a) Show that $v = 4.67 \text{ m s}^{-1}$, correct to three significant figures. (3 marks)
- (b) Find the coefficient of restitution between the spheres. (3 marks)
- (c) Given that the mass of A is 0.5 kg , show that the magnitude of the impulse exerted on A during the collision is 2.17 N s , correct to three significant figures. (3 marks)
- (d) Find the mass of B . (3 marks)

5 A smooth sphere is moving on a smooth horizontal surface when it strikes a smooth vertical wall and rebounds.

Immediately before the impact, the sphere is moving with speed 4 m s^{-1} and the angle between the sphere's direction of motion and the wall is α .

Immediately after the impact, the sphere is moving with speed $v \text{ m s}^{-1}$ and the angle between the sphere's direction of motion and the wall is 40° .

The coefficient of restitution between the sphere and the wall is $\frac{2}{3}$.



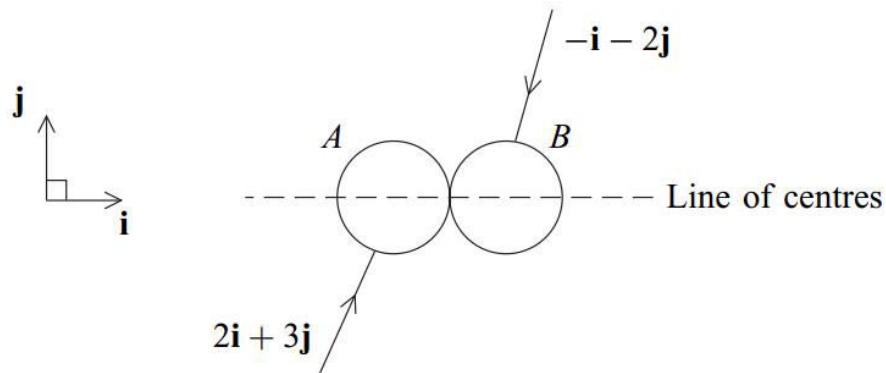
(a) Show that $\tan \alpha = \frac{3}{2} \tan 40^\circ$. *(3 marks)*

(b) Find the value of v . *(3 marks)*

6 Two smooth spheres, A and B , have equal radii and masses 1 kg and 2 kg respectively.

The sphere A is moving with velocity $(2\mathbf{i} + 3\mathbf{j})\text{ m s}^{-1}$ and the sphere B is moving with velocity $(-\mathbf{i} - 2\mathbf{j})\text{ m s}^{-1}$ on the same smooth horizontal surface.

The spheres collide when their line of centres is parallel to the unit vector \mathbf{i} , as shown in the diagram.



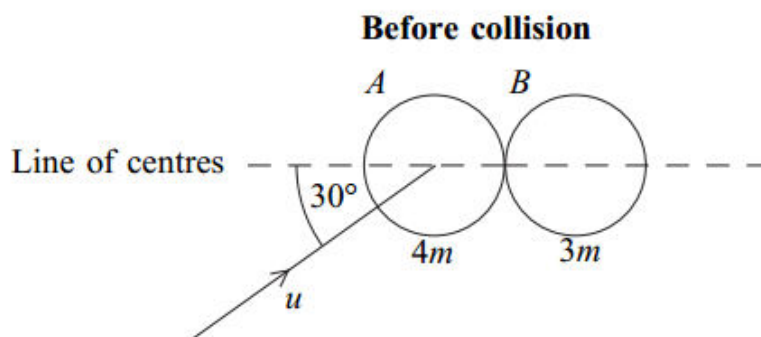
(a) Briefly state why the components of the velocities of A and B parallel to the unit vector \mathbf{j} are not changed by the collision. *(1 mark)*

(b) The coefficient of restitution between the spheres is 0.5 .

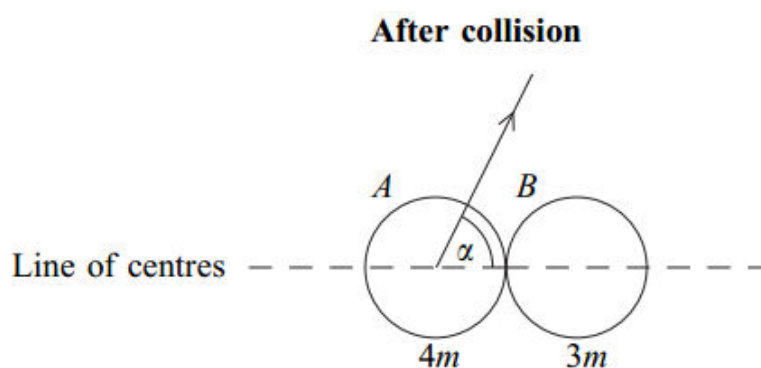
Find the velocities of A and B immediately after the collision. *(6 marks)*

- 7** Two smooth spheres, A and B , have equal radii and masses $4m$ and $3m$ respectively. The sphere A is moving on a smooth horizontal surface and collides with the sphere B , which is stationary on the same surface.

Just before the collision, A is moving with speed u at an angle of 30° to the line of centres, as shown in the diagram below.



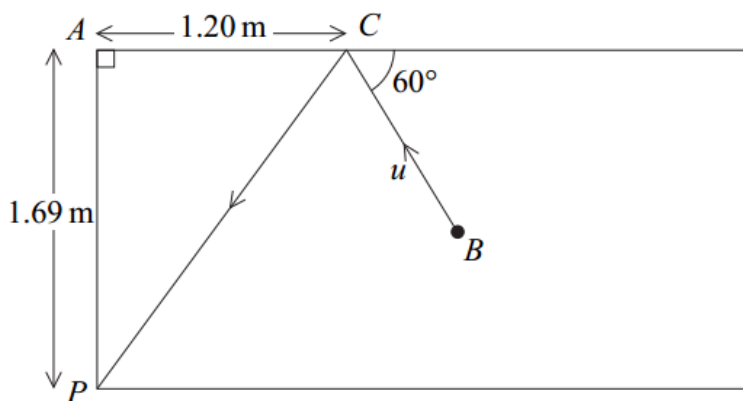
Immediately after the collision, the direction of motion of A makes an angle α with the line of centres, as shown in the diagram below.



The coefficient of restitution between the spheres is $\frac{5}{9}$.

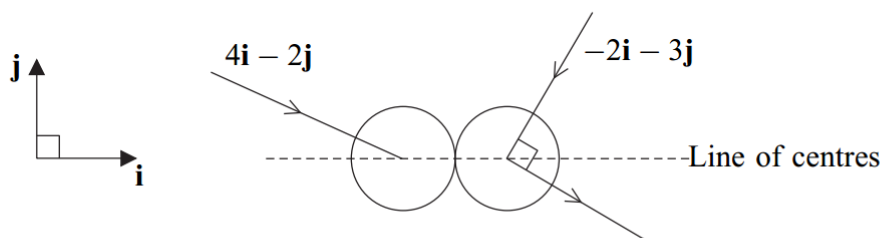
- (a) Find the value of α . (10 marks)
- (b) Find, in terms of m and u , the magnitude of the impulse exerted on B during the collision. (3 marks)

4 The diagram shows part of a horizontal snooker table of width 1.69 m. A player strikes the ball B directly, and it moves in a straight line. The ball hits the cushion of the table at C before rebounding and moving to the pocket at P at the corner of the table, as shown in the diagram. The point C is 1.20 m from the corner A of the table. The ball has mass 0.15 kg and, immediately before the collision with the cushion, it has velocity u in a direction inclined at 60° to the cushion. The **table** and the **cushion** are modelled as smooth.



- (a) Find the coefficient of restitution between the ball and the cushion. (5 marks)
- (b) Show that the magnitude of the impulse on the cushion at C is approximately $0.236u$. (4 marks)
- (c) Find, in terms of u , the time taken between the ball hitting the cushion at C and entering the pocket at P . (3 marks)
- (d) Explain how you have used the assumption that the cushion is smooth in your answers. (1 mark)

6 Two smooth spheres, A and B , have equal radii and masses 4 kg and 2 kg respectively. The sphere A is moving with velocity $(4\mathbf{i} - 2\mathbf{j}) \text{ m s}^{-1}$ and the sphere B is moving with velocity $(-2\mathbf{i} - 3\mathbf{j}) \text{ m s}^{-1}$ on the same smooth horizontal surface. The spheres collide when their line of centres is parallel to unit vector \mathbf{i} . The direction of motion of B is changed through 90° by the collision, as shown in the diagram.



- (a) Show that the velocity of B immediately after the collision is $(\frac{9}{2}\mathbf{i} - 3\mathbf{j}) \text{ m s}^{-1}$. (4 marks)
- (b) Find the coefficient of restitution between the spheres. (5 marks)
- (c) Find the impulse exerted on B during the collision. State the units of your answer. (3 marks)