

Essential skills A* record sheet

Name:

Question	Topic	Worksheet 1	Worksheet 2	Worksheet 3	Worksheet 4	Worksheet 5
1	Completing the square					
2	Sine/cosine rule (lengths)					
3	Surds - Rationalising the denominator					
4	Circle theorems					
5	Forming and solving quadratic equations					
6	Simultaneous equations with quadratic					
7	Rearranging difficult formulae					
8	Algebraic proof					
9	Sine/cosine rule (angles)					
10	Vector geometry					
11	Probability					
12	Simplifying algebraic fractions					
13	Equations involving indices					
14	Transformations of functions					
15	Solving algebraic fraction equations					
	Total					

Keep a record of how well you do in this table.
 You should always try to **improve** on the previous sheet. Make sure you look at your corrections and targets so you know what you have to do to achieve better.

After each sheet, set yourself a target as to what you want to improve for next time..

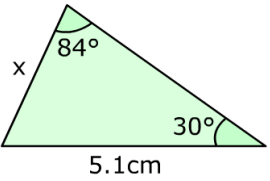
Date Set	Target	Date Achieved

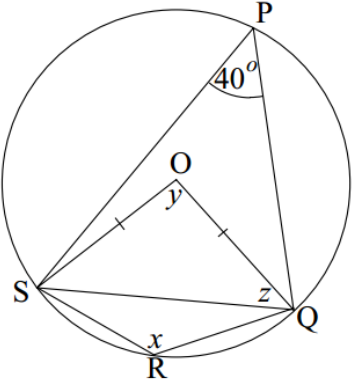

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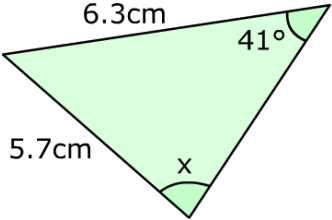
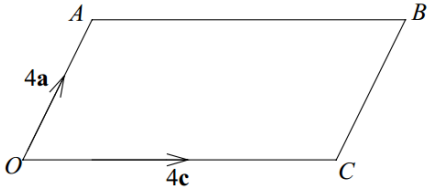
A* GCSE – Essential Skills 1

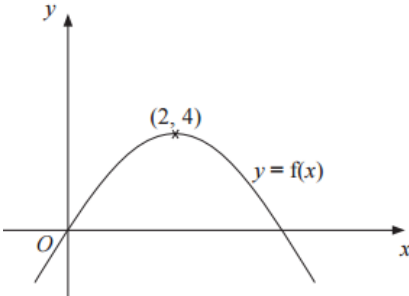
Mark:

Show all of your working out (use a separate sheet if required)

1	<p>Write the following in the form $(x + p)^2 + q$</p> $x^2 + 10x - 20$ <p>Hence find the minimum point of $y = x^2 + 10x - 20$</p>	
2* (104)	<p>Work out the missing length to 3sf</p> 	
3 (95)	<p>Rationalise the denominator:</p> $\frac{15}{\sqrt{3}}$	

<p>4 (90)</p>	<p>Calculate the angles x, y and z</p> 	
<p>5 (98)</p>	<p>The area of the rectangle is 14cm^2. Form a quadratic equation and use it to find the value of x.</p> 	
<p>6* (101)</p>	<p>Solve simultaneous equation (linear/quadratic)</p> $y = 2x + 3$ $y = x^2 + 9x + 15$	
<p>7 (100)</p>	<p>Make m the subject of the formula</p> $3(4p + m) = 5 - 4m$	

<p>8 (111)</p>	<p>Prove that half the sum of four consecutive numbers is odd.</p>	
<p>9* (104)</p>	<p>Work out the missing angle to the nearest degree</p> 	
<p>10 (108)</p>	<p>Find in terms of \mathbf{a} and \mathbf{c} \overrightarrow{AP} where P is the midpoint of AC</p> 	
<p>11 (92)</p>	<p>A bag contains 3 black discs and 7 white discs. A disc is taken at random from the bag and not replaced. Another disc is then taken. Find the probability that both discs were black. (Draw tree diagram on separate sheet if required)</p>	

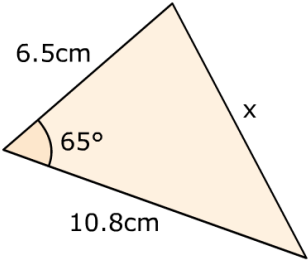
<p>12 (99)</p>	<p>Simplify fully</p> $\frac{x^2 + 4x}{4x + 16}$	
<p>13 (94)</p>	<p>Find the value of $64^{-\frac{2}{3}}$</p>	
<p>14 (102)</p>	 <p>Write down the maximum point of $y = f(x-5) + 2$</p>	
<p>15* (99)</p>	<p>Solve the following equation:</p> $x + \frac{2}{x} = 3$	

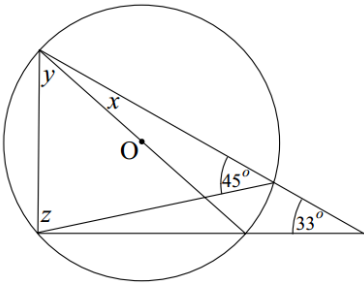

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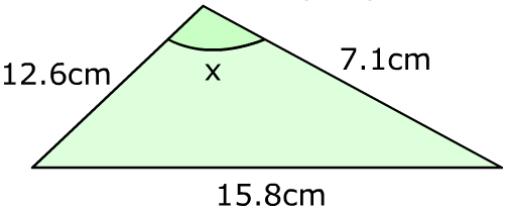
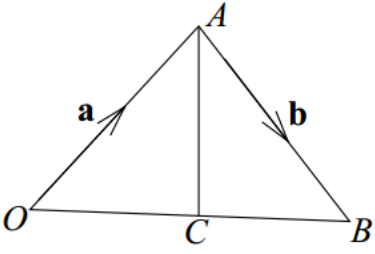
A* GCSE – Essential Skills 2

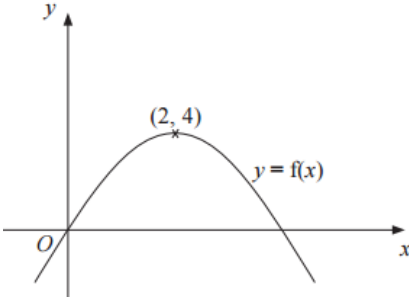
Mark:

Show all of your working out (use a separate sheet if required)

1	<p>Write the following in the form $(x + p)^2 + q$</p> $x^2 + 6x + 12$ <p>Hence find the minimum point of $y = x^2 + 6x + 12$</p>	
2* (104)	<p>Work out the missing length to 3sf</p>  <p>The diagram shows a right-angled triangle with an angle of 65° at the top-left vertex. The side adjacent to this angle is labeled 6.5cm. The side opposite to this angle is labeled 10.8cm. The hypotenuse is labeled x.</p>	
3 (95)	<p>Rationalise the denominator:</p> $\frac{16}{3 + \sqrt{5}}$	

<p>4 (90)</p>	<p>Calculate the angles x, y and z</p> 	
<p>5 (98)</p>	<p>The area of the rectangle is 63cm^2. Form a quadratic equation and use it to find the value of x.</p> <p>$(x + 4)\text{cm}$</p>  <p>$(2x - 7)\text{cm}$</p>	
<p>6* (101)</p>	<p>Solve simultaneous equation (linear/quadratic)</p> $x^2 + y^2 = 20$ $y = 3x - 10$	
<p>7 (100)</p>	<p>Make x the subject of the formula</p> $3(x - 4) = y(5 - 2x)$	

<p>8 (111)</p>	<p>Prove that: $(n+4)^2 - (3n+4) \equiv (n+1)(n+4) + 8$</p>	
<p>9* (104)</p>	<p>Work out the missing angle to the nearest degree</p>  <p>The diagram shows a triangle with a base of 15.8cm. The left side is 12.6cm and the right side is 7.1cm. The angle at the top vertex is labeled 'x'.</p>	
<p>10 (108)</p>	<p>C is the midpoint of OB. Find \overrightarrow{AC} in terms of a and b.</p>  <p>The diagram shows a triangle with vertices O, A, and B. Point C is on the base OB. Vectors a and b are drawn from O to A and from A to B respectively.</p>	
<p>11 (92)</p>	<p>A bag contains 2 red balls and 7 blue balls. A ball is taken at random from the bag and not replaced. Another ball is then taken. Find the probability that both balls were the same colour. (Draw tree diagram on separate sheet if required)</p>	

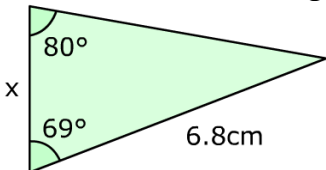
<p>12 (99)</p>	<p>Simplify fully</p> $\frac{3x - 21}{x^2 + x - 56}$	
<p>13 (94)</p>	<p>Find the value of x</p> $\left(\frac{1}{2}\right)^x = 32$	
<p>14 (102)</p>	 <p>Write down the maximum point of $y = f(2x) - 3$</p>	
<p>15* (99)</p>	<p>Solve the following equation:</p> $\frac{x - 3}{2} = \frac{5}{x}$	

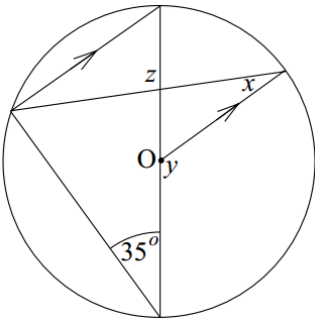
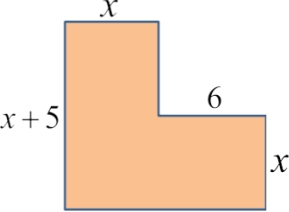
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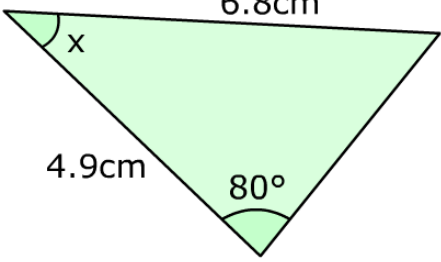
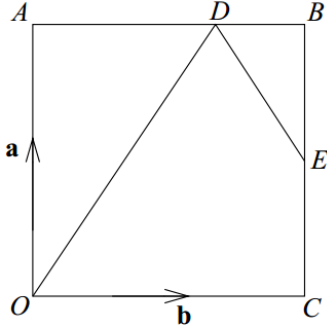
A* GCSE – Essential Skills 3

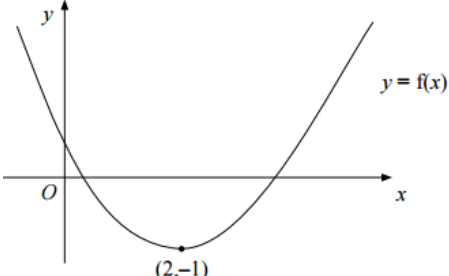
Mark:

Show all of your working out (use a separate sheet if required)

1	<p>Write the following in the form $(x + p)^2 + q$</p> $x^2 + 16x + 64$ <p>Hence find the minimum point of $y = x^2 + 16x + 64$</p>	
2* (104)	<p>Work out the missing length to 3sf</p> 	
3 (95)	<p>Rationalise the denominator:</p> $\frac{20}{5 - \sqrt{5}}$	

<p>4 (90)</p>	<p>Calculate the angles x,y and z</p> 	
<p>5 (98)</p>	<p>The area of the shape is 60cm^2. Form a quadratic equation and use it to find the value of x.</p> 	
<p>6* (101)</p>	<p>Solve simultaneous equation (linear/quadratic)</p> $y = x^2 + 8x - 6$ $y = 3x + 8$	
<p>7 (100)</p>	<p>Make c the subject of the formula</p> $a = \frac{3bc}{b - c}$	

<p>8 (111)</p>	<p>Prove that, if the difference of two numbers is 4, then the difference of their squares is a multiple of 8.</p>	
<p>9* (104)</p>	<p>Work out the missing angle to the nearest degree</p> 	
<p>10 (108)</p>	 <p>OABC is a square. Point D cuts the line AB in the ratio 2:1. Point E is the midpoint of BC. By first finding \overline{OD} and \overline{OE}, find the vector \overline{DE}</p>	
<p>11 (92)</p>	<p>There are 3 digestives and 5 custard creams in a biscuit tin. Oakley takes two at random. Work out the probability that she gets one of each. (Draw tree diagram on separate sheet if required)</p>	

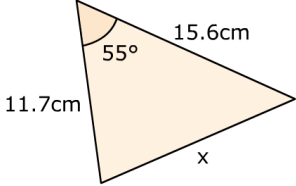
<p>12 (99)</p>	<p>Simplify fully</p> $\frac{x^2 - 2x - 24}{x^2 + 8x + 16}$	
<p>13 (94)</p>	<p>Find the value of x</p> $2^x = \frac{1}{16}$	
<p>14 (102)</p>	 <p>Write down the minimum point of $y = f(x-4) + 3$</p>	
<p>15* (99)</p>	<p>Solve the following equation:</p> $\frac{5x+4}{x+2} - \frac{3}{x} = 2$	

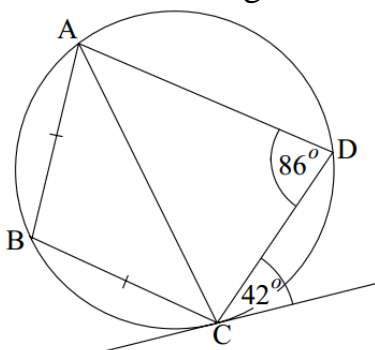
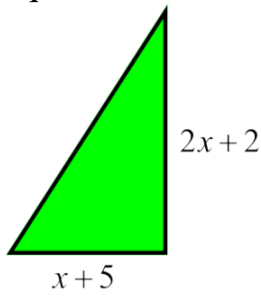
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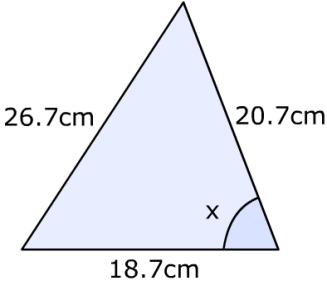
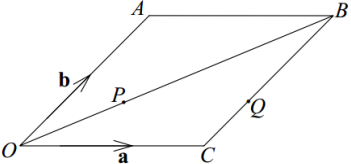
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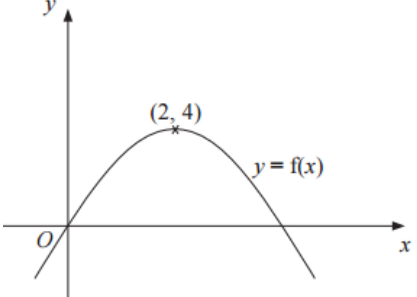
Mark:

Show all of your working out (use a separate sheet if required)

1	<p>Write the following in the form $(x + p)^2 + q$</p> $x^2 + 5x - 6$ <p>Hence find the minimum point of $y = x^2 + 5x - 6$</p>	
2* (104)	<p>Work out the missing length to 3sf</p>  <p>The diagram shows a triangle with a top vertex angle of 55°. The left side is labeled 11.7cm, the right side is labeled 15.6cm, and the bottom side is labeled x.</p>	
3 (95)	<p>Rationalise the denominator:</p> $\frac{9}{2 + \sqrt{3}}$	

<p>4 (90)</p>	<p>Calculate the angles ABC, ACB, ACD and DAC</p> 	
<p>5 (98)</p>	<p>The area of the triangle is 21cm^2. Form a quadratic equation and use it to find the value of x.</p> 	
<p>6* (101)</p>	<p>Solve simultaneous equation (linear/quadratic)</p> $y = x^2 + 6x + 11$ $y = 10x + 8$	
<p>7 (100)</p>	<p>Make n the subject of the formula</p> $m = \frac{5 - 3n}{2n - 4}$	

<p>8 (111)</p>	<p>Prove that: $(n+3)^2 - (3n+5) \equiv (n+1)(n+2) + 2$</p>	
<p>9* (104)</p>	<p>Work out the missing angle to the nearest degree</p> 	
<p>10 (108)</p>	 <p>OABC is a rhombus. Point P cuts the line OB in the ratio 1:2. Point Q cuts the line CB in the ratio 1:2. Find the vector \overrightarrow{PQ} and explain why it is parallel to \overline{AB}.</p>	
<p>11 (92)</p>	<p>In a class of 20 pupils there are 6 boys and 14 girls. Two names are chosen at random. Find the probability that they are both girls. (Draw tree diagram on separate sheet if required)</p>	

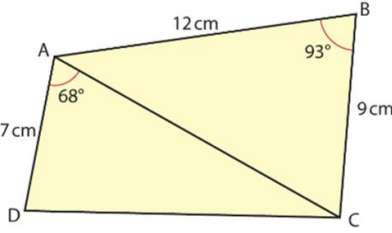
<p>12 (99)</p>	<p>Simplify fully</p> $\frac{x^2 + x - 6}{x^2 - 7x + 10}$	
<p>13 (94)</p>	<p>Find the value of x</p> $25^x = \frac{1}{5}$	
<p>14 (102)</p>	 <p>Write down the maximum point of $y = f(-2x)$</p>	
<p>15* (99)</p>	<p>Solve the following equation:</p> $\frac{3}{x-2} + \frac{8}{x+3} = 2$	

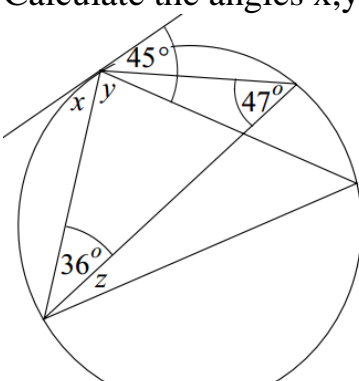
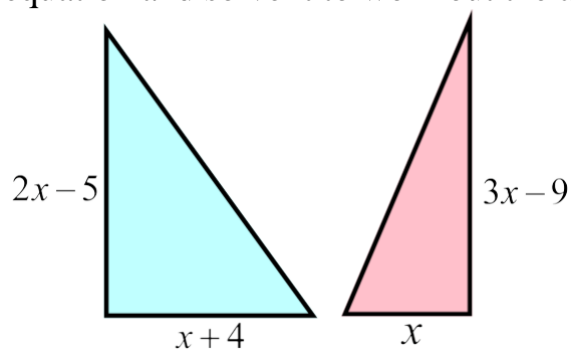
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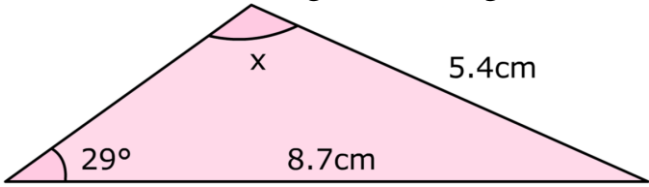
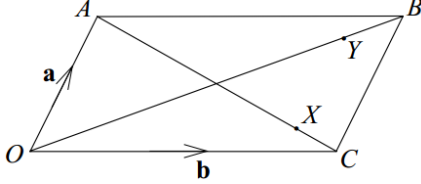
A* GCSE – Essential Skills 5

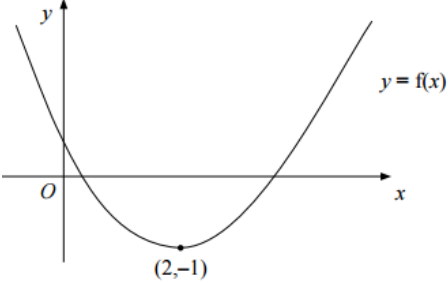
Mark:

Show all of your working out (use a separate sheet if required)

1	<p>Write the following in the form $(x + p)^2 + q$</p> $x^2 + \frac{1}{2}x + 2$ <p>Hence find the minimum point of $y = x^2 + \frac{1}{2}x + 2$</p>	
2* (104)	<p>Find the length DC to 3sf</p>  <p>The diagram shows a quadrilateral ABCD with vertices A, B, C, and D. Side AB is 12 cm, side BC is 9 cm, and side AD is 7 cm. Angle B is 93 degrees and angle A is 68 degrees. Diagonal AC is drawn, dividing the quadrilateral into two triangles, ABC and ADC.</p>	
3 (95)	<p>Rationalise the denominator:</p> $\frac{21}{3 - \sqrt{7}}$	

<p>4 (90)</p>	<p>Calculate the angles x, y and z</p> 	
<p>5 (98)</p>	<p>The areas of both rectangles are equal. Form a quadratic equation and solve it to work out the area of each triangle.</p> 	
<p>6* (101)</p>	<p>Solve simultaneous equation (linear/quadratic)</p> $x^2 + y^2 = 52$ $y = x - 2$	
<p>7 (100)</p>	<p>Make x the subject of the formula</p> $\frac{1}{x} + \frac{1}{y} = \frac{1}{z}$	

<p>8 (111)</p>	<p>Prove that $(3n+1)^2 - (3n-1)^2$ is a multiple of 6 for all values of n.</p>	
<p>9* (104)</p>	<p>Work out the missing obtuse angle to the nearest degree</p> 	
<p>10 (108)</p>	 <p>OACB is a parallelogram. Point Y and point X cut the lines OB and OC in the ratio 5:1. Find the vectors \overrightarrow{OB}, \overrightarrow{YB}, \overrightarrow{AC}, \overrightarrow{XC} and \overrightarrow{XY}. How are XY and CB related?</p>	
<p>11 (92)</p>	<p>There are 3 red sweets, 2 green sweets and 5 blue sweets in a bag. Shona eats 2 random sweets. What is the probability that both sweets were the same colour? (Draw tree diagram on separate sheet if required)</p>	

<p>12 (99)</p>	<p>Simplify fully</p> $\frac{x^2 + 4x - 32}{x^2 - 8x + 16}$	
<p>13 (94)</p>	<p>Find the value of x</p> $81^x = \frac{1}{3}$	
<p>14 (102)</p>	 <p>Write down the minimum point of $y = 3f(x-2)$</p>	
<p>15* (99)</p>	<p>Solve the following equation:</p> $\frac{5}{x+2} + \frac{2}{x-1} = 1$	