Name: Answers

Exam Style Questions

Composite Functions Inverse Functions



Ensure you have: Pencil, pen, ruler, protractor, pair of compasses and eraser

You may use tracing paper if needed

Guidance

- 1. Read each question carefully before you begin answering it.
- 2. Don't spend too long on one question.
- 3. Attempt every question.
- 4. Check your answers seem right.
- 5. Always show your workings

Revision for this topic

www.corbettmaths.com/contents

Video 369 Video 370



1. Given
$$f(x) = \frac{2x+1}{3}$$

(a) Calculate the value of f(7)

$$f(7) = \frac{2(7)+1}{3} = \frac{15}{3} = 5$$

(1)(b) Find $f^{-1}(x)$

x->+1->+3->f(2)

$$f'(x) \leftarrow \div 2 \leftarrow -1 \leftarrow \times 3 \leftarrow \infty$$

$$\frac{3x-1}{2} \qquad 3x-1 \qquad 3x$$

$$f^{-1}(x) = \frac{3x-1}{2}$$

The functions f(x) and g(x) are given by the following: 2.

$$f(x) = 3x - 1$$
$$g(x) = 2x + 4$$

(a) Calculate the value of fg(2)

$$9(2) = 2(2) + 4 = 8$$

 $f(8) = 3(8) - 1 = 23$

(2)

(b) Calculate the value of ff(3)

(c) Find gf(x)

$$9f(x) = 2[3x-1]+4$$

= $6x-1+4$
= $6x+1$

3. The functions f(x), g(x) and h(x) are given by the following:

$$f(x) = x^{2} - 3$$
$$g(x) = 2x + 1$$
$$h(x) = \frac{x}{2}$$

(a) Find
$$fg(x)$$

$$f9(x) = (2x+1)^2 - 3$$

= $4x^2 + 4x + 1 - 3$

(b) Find
$$gh(x)$$

 $gh(x) = 2(\frac{x}{2}) + 1$
 $= x + 1$

(c) Find $f^{-1}(x)$

4. The function f is such that f(x) = 4x - 7

(a) Solve
$$f(x) = 17$$

$$|4x-7=17|$$

 $|4x=24|$
 $|4x=24|$
 $|4x=6|$

(b) Find
$$f^{-1}(x)$$

$$x \rightarrow x4 \rightarrow -7 \rightarrow f(x)$$

$$f'(x) \leftarrow \div 4 \leftarrow +7 \leftarrow x$$

$$\frac{x+7}{4} \qquad x+7$$

$$f^{-1}(x) = \frac{x+7}{4}$$

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5. Given
$$f(x) = x^2 + 2$$
 and $g(x) = x + 14$

Find the values of a such that f(a) = g(a)

$$a^{2}+2=a+14$$
 $a^{2}-a-12=0$
 $(a-4)(a+3)=0$
 $a=4$ $a=-3$

$$0=4 \qquad 0=-3$$

6. The functions f(x) and g(x) are given by the following:

$$f(x) = 8 - 3x$$
$$g(x) = 4x$$

(a) Calculate the value of gf(3)

(b) Solve the equation gf(x) = 80

$$31-11x = 80$$

 $-12x = 48$
 $x = -4$

7.
$$f(x) = 2x^2 - 1$$

Find $f^{-1}(x)$

$$x \rightarrow squared \rightarrow x2 \rightarrow -1 \rightarrow fa$$

$$f^{-1}(x) \leftarrow root \leftarrow +1 \leftarrow x \qquad f^{-1}(x) = \sqrt{\frac{x+1}{2}} \qquad x+1 \qquad x+1 \qquad (3)$$

8. Given
$$f(x) = x^2 + 3x - 5$$

Express f(2x-1) in the form $ax^2 + bx + c$

$$f(2x-1) = (2x-1)^{2} + 3(2x-1) - 5$$

$$= [4x^{2} - 4x + 1] + [6x - 3] - 5$$

$$= 4x^{2} + 2x - 7$$

$$4x^2+2x-7$$

9. The function f is such that
$$f(x) = kx + 3$$

The function g is such that g(x) = 2x - 4

Given that gf(2) = 34

work out the value of k

$$f(2) = 2k+3$$

 $g(2k+3) = 2[2k+3]-4$
 $g(2k+3) = 4k+2$
 $4k+2=34$
 $4k=32$
 $V=8$

10. For all values of x,

$$f(x) = x^2 + 4$$
$$g(x) = x - 9$$

Solve fg(x) = gf(x)

$$f9(x) = (x-9)^{2} + 4$$

= $x^{2} - 18x + 85$
 $9(x) = (x^{2} + 4) - 9$
= $x^{2} - 5$

$$x^{2}-18x+85=x^{2}-5$$
 $18x=90$
 $x=5$

$$X = 5$$

11.
$$f(x) = x^2 + 2x + 1$$

Show that
$$f(x+2) - f(x) = 4x + 8$$

$$f(x+2) = (x+2)^{2} + 2(x+2) + 1$$

$$f(x+1) = [x^{2} + 4x + 4] + [2x+4] + 1$$

$$f(x+1) = x^{2} + 6x + 9$$

$$f(x+1) - f(x) = [x^{2} + 6x + 9] - [x^{2} + 2x + 1]$$

$$= x^{2} + 6x + 9 - x^{2} - 2x - 1$$

$$= 4x + 8$$

(3)